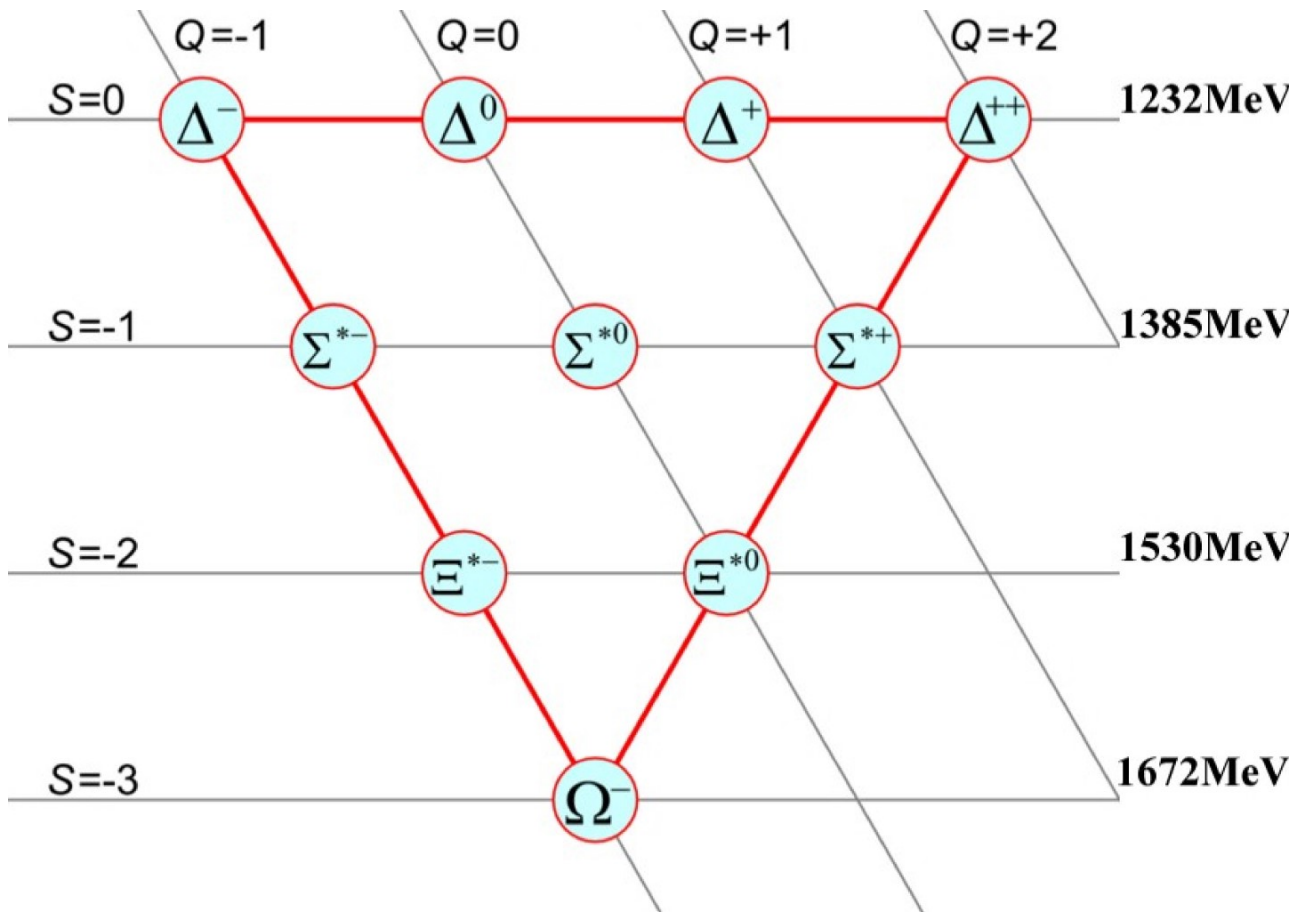


# Quantum gravity from fakeons

*Damiano Anselmi*



- How the idea of fake particle ("fakeon") leads to what I claim is the right theory of quantum gravity
- Physical implications and predictions
- Classical limit
- FLRW solution
- Cosmology

The problem of quantum gravity is to make it renormalizable and unitary at the same time

$$\frac{1}{(p^2 - m_1^2)(p^2 - m_2^2)} = \frac{1}{m_1^2 - m_2^2} \left[ \frac{1}{p^2 - m_1^2} - \frac{1}{p^2 - m_2^2} \right]$$

Higher derivatives lead to renormalizability, but violate unitarity, unless ...

Unitarity:  $S^\dagger S = 1$

$$S = 1 + iT$$

$$2\text{Im}T = T^\dagger T \quad \text{Optical theorem}$$

$$\frac{1}{2i} [\langle b|T|a\rangle - \langle b|T^\dagger|a\rangle] = \sum_{|n\rangle \in W} \underbrace{(-1)^{\sigma_n}}_{\sigma_n = 0, 1} \langle b|T^\dagger|n\rangle \langle n|T|a\rangle, \quad |a\rangle, |b\rangle \in W$$

In general,  $W$  may contain unphysical states in higher-derivative theories (those with  $\sigma_n = 1$ )  
Feynman prescription  $\rightarrow$  pseudounitariness equation

Diagrammatic version of the optical theorem:

$$2\text{Im} \left[ (-i) \text{Y} \text{---} \text{Y} \right] = \text{Y} \text{---} \text{Y} = \int d\Pi_f \left| \text{Y} \text{---} \right|^2$$

$$2\text{Im} \left[ (-i) \text{---} \bigcirc \text{---} \right] = \text{---} \bigcirc \text{---} = \int d\Pi_f \left| \text{---} \text{Y} \right|^2$$

cutting equations

Propagator:

$$G(p, m) = \frac{1}{p^2 - m^2}$$

A prescription  
is needed

The Feynman  
prescription gives

$$G_+(p, m, \epsilon) = \frac{1}{p^2 - m^2 + i\epsilon}$$

The optical theorem is ok:

$$2\text{Im} \left[ (-i) \text{Y} \text{---} \text{Y} \right] = \text{Y} \text{---} \text{Y} = \int d\Pi_f \left| \text{Y} \text{---} \right|^2 \geq 0$$

Indeed:

$$\text{Im} \left[ -\frac{1}{p^2 - m^2 + i\epsilon} \right] = \pi \delta(p^2 - m^2) \geq 0$$

Ghost: opposite residue

$$-\frac{1}{p^2 - m^2 + i\epsilon}$$

The optical theorem is violated

Note that the prescription is crucial

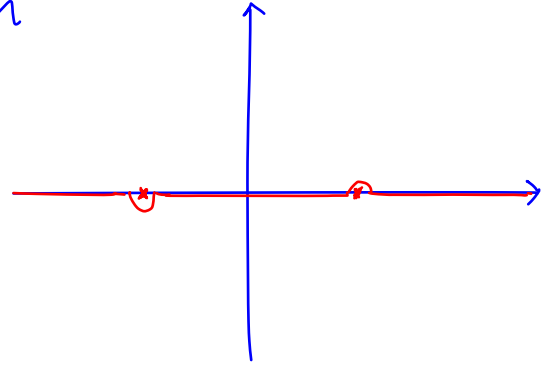
$$-\frac{1}{p^2 - m^2 - i\epsilon}$$

would be ok

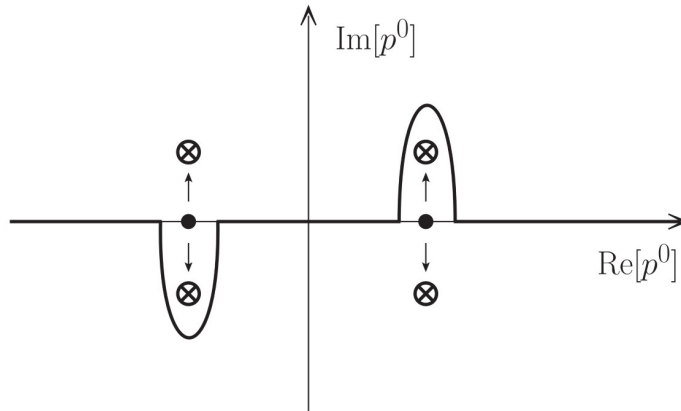
Correct answer: the poles

$LP^0$

$$G(p, m) = \frac{1}{p^2 - m^2}$$



Write  $\pm \frac{p^2 - m^2}{(p^2 - m^2)^2}$  and split the poles into pairs





This is achieved by inserting an infinitesimal width as follows :

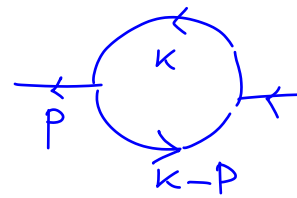
$$G_{\pm}(p, m, \mathcal{E}^2) = \pm \frac{p^2 - m^2}{(p^2 - m^2)^2 + \mathcal{E}^4}$$

Note that the residue is zero on shell :


⇒ NO PARTICLE

However, the story is NOT that simple...

Example: bubble diagram



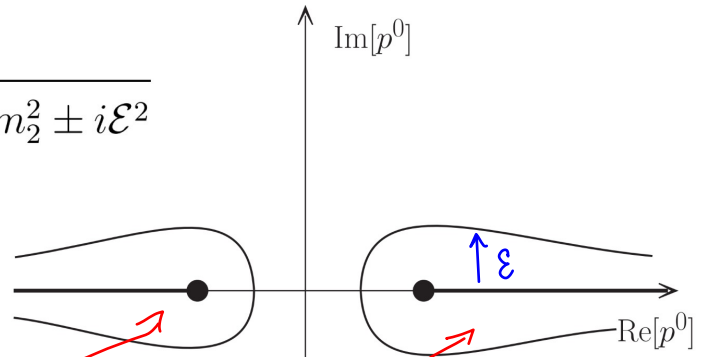
$$i\mathcal{M} \propto \int \frac{dk^0}{2\pi} \int_{\mathbb{R}^3} \frac{d^3\mathbf{k}}{(2\pi)^3} \mathbb{G}_{\pm}(p-k, m_1, \mathcal{E}^2) \mathbb{G}_{\pm}(k, m_2, \mathcal{E}^2)$$

  
 LW

$$= \int_{\mathbb{R}^3} \frac{d^3\mathbf{k}}{(2\pi)^3} w(p, \mathbf{k})$$

$w(p, \mathbf{k})$  is singular for

$$|p^0| = \sqrt{(\mathbf{p} - \mathbf{k})^2 + m_1^2 \pm i\mathcal{E}^2} + \sqrt{\mathbf{k}^2 + m_2^2 \pm i\mathcal{E}^2}$$

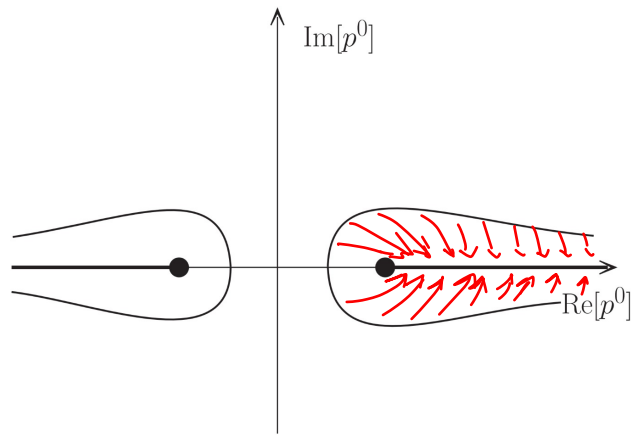
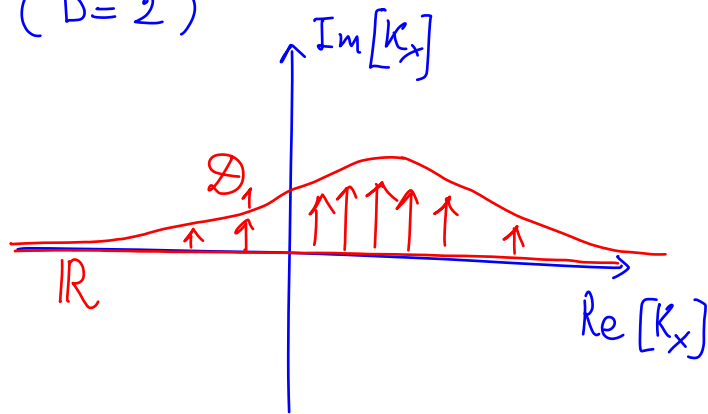


Here Lorentz invariance & analyticity are violated

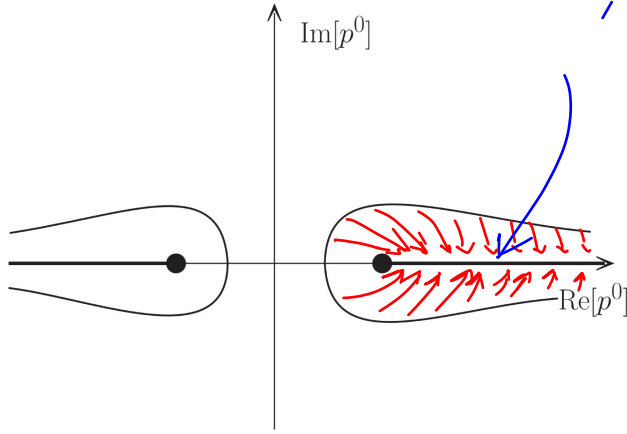
The integration domain on the loop space momentum must be deformed

$$\int_{\mathbb{R}^3} \frac{d^3 \mathbf{k}}{(2\pi)^3} w(p, \mathbf{k}) \longrightarrow \int_{\mathcal{D}_3} \frac{d^3 \mathbf{k}}{(2\pi)^3} w(p, \mathbf{k})$$

Deformation:  $\mathbb{R} \rightarrow \mathcal{D}_1$   
( $D=2$ )



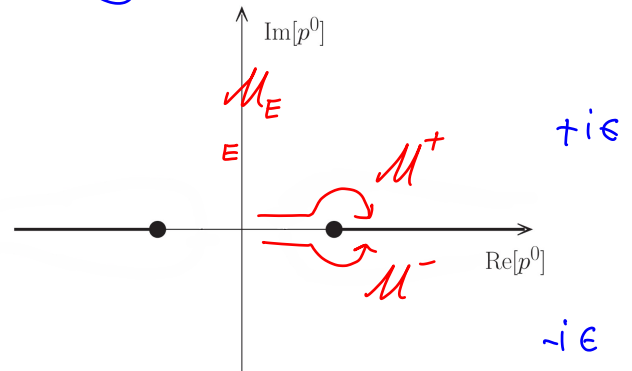
calculate  
INSIDE, then deform the domain  
 (and, possibly,  
 take  $\epsilon \rightarrow 0$ )



Lorentz invariance and analyticity are recovered  
 in the limit

Result: average continuation

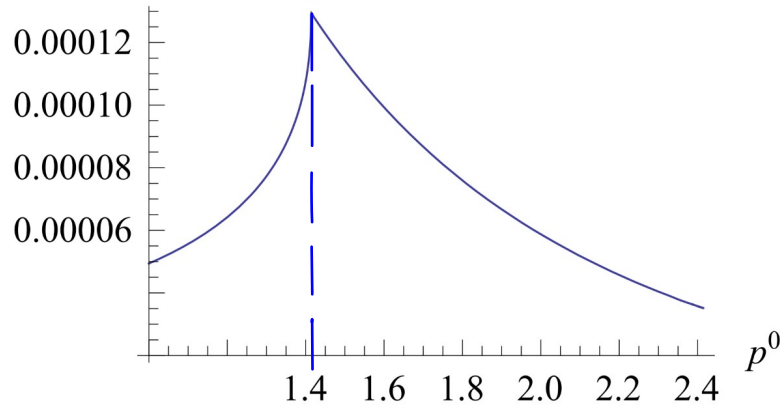
$$\frac{1}{2} (M^+ + M^-)$$



Result :

$\text{Re} [(-i)-0]$  fake  
threshold

$\text{Im} [(-i)-0] = 0$



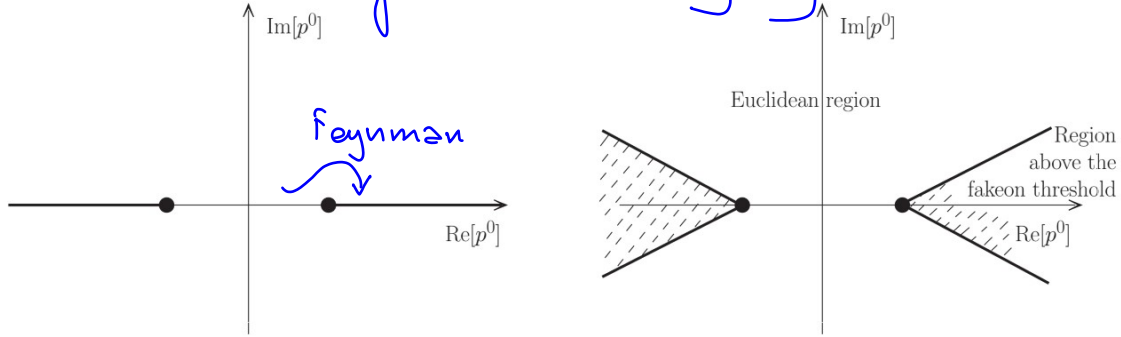
Feynman :

$$\int_0^1 dx \ln [-p^2 x(1-x) + m^2 - i\epsilon]$$

Fakeon :

$$\frac{1}{2} \int_0^1 dx \ln [(-p^2 x(1-x) + m^2)^2]$$

# Region wise analyticity



Since the prescription is symmetric w.r.t. the real axis, the imaginary part of the amplitude vanishes:

$$0 = 2\text{Im} \left[ (-i) \text{---} \text{---} \text{---} \begin{array}{c} \text{F} \\ \bigcirc \\ \text{F} \end{array} \text{---} \text{---} \right] = \text{---} \begin{array}{c} \text{F} \\ \bigcirc \\ \text{F} \end{array} \text{---} = \int d\Pi_f \left| \begin{array}{c} \text{In} \\ \text{F} \\ \text{F} \end{array} \right|^2 = 0$$

$\int_{\text{fakeon}}$

$\Rightarrow$  the fakeon F MUST be projected away :

From

$$\frac{1}{2i} [\langle b|T|a\rangle - \langle b|T^\dagger|a\rangle] = \sum_{|n\rangle \in W} \langle b|T^\dagger|n\rangle \langle n|T|a\rangle, \quad |a\rangle, |b\rangle \in W$$

~~$(-1)^n$~~   $1, 0$

to

$$\frac{1}{2i} [\langle b|T|a\rangle - \langle b|T^\dagger|a\rangle] = \sum_{|n\rangle \in V} \langle b|T^\dagger|n\rangle \langle n|T|a\rangle, \quad |a\rangle, |b\rangle \in V$$

with  $V \subset W$ ,  $|F\rangle \in W$ ,  $|F\rangle \notin V$

To all orders:

D. Anselmi (2018), Fakeons & Lee-Wick models, JHEP

# Quantum gravity

D. Anselmi, On the quantum field theory of the gravitational interactions, J. High Energy Phys. 06 (2017) 086, 17A3 Renormalization.com and arXiv:1704.07728 [hep-th].

Consider the (renormalizable) higher-derivative action  
 $\zeta, \alpha, \xi > 0$

$$S_{\text{QG}} = -\frac{1}{2\kappa^2} \int \sqrt{-g} \left[ 2\Lambda_C + \zeta R + \alpha \left( R_{\mu\nu} R^{\mu\nu} - \frac{1}{3} R^2 \right) - \frac{\xi}{6} R^2 \right] + S_{\text{m}}(g, \Phi)$$

Eliminate the higher derivatives by means of extra fields :

D. Anselmi and M. Piva, Quantum gravity, fakeons and microcausality, J. High Energy Phys. 11 (2018) 21, 18A3 Renormalization.com and arXiv:1806.03605 [hep-th].

$$S_{\text{QG}}(g, \phi, \chi, \Phi) = S_{\text{H}}(g) + S_{\chi}(g, \chi) + S_{\phi}(\tilde{g}, \phi) + S_{\text{m}}(\tilde{g} e^{\kappa\phi}, \Phi)$$

where  $\tilde{g}_{\mu\nu} = g_{\mu\nu} + 2\chi_{\mu\nu}$

$$S_{\text{H}}(g) = -\frac{\zeta}{2\kappa^2} \int \sqrt{-g} R, \quad S_{\phi}(g, \phi) = \frac{3\zeta}{4} \int \sqrt{-g} \left[ \nabla_{\mu} \phi \nabla^{\mu} \phi - \frac{m_{\phi}^2}{\kappa^2} (1 - e^{\kappa\phi})^2 \right]$$

$$S_{\chi}(g, \chi) = S_{\text{H}}(\tilde{g}) - S_{\text{H}}(g) - 2 \int \chi_{\mu\nu} \frac{\delta S_{\text{H}}(\tilde{g})}{\delta g_{\mu\nu}} + \frac{\zeta^2}{2\alpha\kappa^2} \int \sqrt{-g} (\chi_{\mu\nu} \chi^{\mu\nu} - \chi^2) \Big|_{g \rightarrow \tilde{g}}.$$



Now, the  $\chi_{\mu\nu}$  action has the wrong overall sign:

$$S_\chi(g, \chi) = -\frac{\zeta}{\kappa^2} S_{\text{PF}}(g, \chi, m_\chi^2) - \frac{\zeta}{2\kappa^2} \int \sqrt{-g} R^{\mu\nu} (\chi\chi_{\mu\nu} - 2\chi_{\mu\rho}\chi_\nu^\rho) + S_\chi^{(>2)}(g, \chi)$$

where  $S_{\text{PF}}$  is the covariantized Pauli-Fierz action

This means that  $\chi_{\mu\nu}$  MUST be quantized as a fakeon. This way, we have both renormalizability and unitarity.

Instead,  $\phi$  can be quantized either as a fakeon or as a physical particle

Graviton multiplet:  $\{h_{\mu\nu}, \phi, \chi_{\mu\nu}\}$

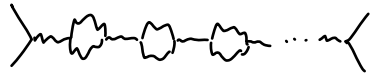
$$g_{\mu\nu} = \eta_{\mu\nu} + 2\kappa h_{\mu\nu}$$

fluctuation of the metric

massive scalar

spin-2  
fakeon of mass  $m_\chi$

$$m_\chi = \frac{J}{\alpha}$$



Fakeon width:

$$\Gamma_\chi = -\alpha_\chi C m_\chi$$

$\Gamma_\chi < 0$ : causality is violated by  $\chi_{\mu\nu}$

$$C = \frac{N_s + 6N_f + 12N_v}{120}$$

$$\alpha_\chi = \left(\frac{m_\chi}{M_{\text{Pl}}}\right)^2$$

	Fermions			Bosons	
Quarks	$u$	$c$	$t$	$\gamma$	$H$
	$d$	$s$	$b$	$W^\pm$	$g$
Leptons	—————			$Z^0$	$\phi$
	$e$	$\mu$	$\tau$	$g$	$\chi$
	$\nu_e$	$\nu_\mu$	$\nu_\tau$		

A blue bracket groups  $\phi$ ,  $Z^0$ , and  $g$  with the label "QG triplet".  
 A blue arrow points from the bracket to the text "fakeon?".  
 A blue bracket groups  $\chi$  and  $g$  with the label "fakeon".

The fields of the standard model and quantum gravity could explain everything we know

# PROJECTION

At the level of generating functionals:

$$\Gamma(\varphi, \chi)$$

$\varphi =$  physical fields

$\chi =$  fakeons

Solve  $\delta\Gamma(\varphi, \chi)/\delta\chi = 0$  by means of the fakeon prescription

Let  $\langle\chi\rangle$  denote the solution

Projected functionals:

$$\Gamma_{\text{pr}}(\varphi) = \Gamma(\varphi, \langle\chi\rangle)$$

$$Z_{\text{pr}}(J) = \int [d\varphi d\chi] \exp\left(iS(\varphi, \chi) + i \int J\varphi\right) = \exp(iW_{\text{pr}}(J))$$

NO SOURCE  $J_\chi$  FOR  $\chi$

Projection = integrating out the fakeons with the fakeon prescription

Classical limit : Set of tree diagrams with  
NO fakeon external legs

The starting action

$$S_{\text{QG}}(g, \phi, \chi, \Phi) = S_{\text{H}}(g) + S_{\chi}(g, \chi) + S_{\phi}(\tilde{g}, \phi) + S_{\text{m}}(\tilde{g}e^{\kappa\phi}, \Phi)$$

is NOT the classical limit, because it  
is unprojected

→ INTERIM classical action : LOCAL

E.g. : 
$$\mathcal{L}_{\text{gf}} = -\frac{1}{4} F_{\mu\nu}^2 + \frac{1}{2\lambda} (\partial \cdot A)^2 + \bar{C} \partial DC$$

gauge-fixed Lagrangian : unprojected, but LOCAL

Unprojected field equations :

$$g_{\mu\nu} : \quad R^{\mu\nu} - \frac{1}{2}g^{\mu\nu}R = \frac{\kappa^2}{\zeta} [e^{3\kappa\phi} fT_m^{\mu\nu}(\tilde{g}e^{\kappa\phi}, \Phi) + fT_\phi^{\mu\nu}(\tilde{g}, \phi) + T_\chi^{\mu\nu}(g, \chi)].$$

$$\phi : \quad -\frac{1}{\sqrt{-\tilde{g}}} \partial_\mu (\sqrt{-\tilde{g}} \tilde{g}^{\mu\nu} \partial_\nu \phi) - \frac{m_\phi^2}{\kappa} (e^{\kappa\phi} - 1) e^{\kappa\phi} = \frac{\kappa e^{3\kappa\phi}}{3\zeta} T_m^{\mu\nu}(\tilde{g}e^{\kappa\phi}, \Phi) \tilde{g}_{\mu\nu},$$

$$\chi_{\mu\nu} : \quad \frac{1}{\sqrt{-g}} \frac{\delta S_\chi(g, \chi)}{\delta \chi_{\mu\nu}} = e^{3\kappa\phi} fT_m^{\mu\nu}(\tilde{g}e^{\kappa\phi}, \Phi) + fT_\phi^{\mu\nu}(\tilde{g}, \phi),$$

Projection : solve the  $\chi$  field equation (with the fakeon prescription) and insert the solution into the other equations

At the tree level, the subtleties about integration paths and average continuations are not important,

so we can take

$$\frac{p^2 - m^2}{(p^2 - m^2)^2 + \mathcal{E}^4} = \mathcal{P} \frac{1}{p^2 - m^2}$$

Use it to solve the fakeon equations

The projected classical action is then

$$\mathcal{S}_{\text{QG}}(g, \phi, \Phi) = S_{\text{H}}(g) + S_{\chi}(g, \langle \chi \rangle) + S_{\phi}(\bar{g}, \phi) + S_{\text{m}}(\bar{g} e^{\kappa \phi}, \Phi)$$

where  $\langle \chi \rangle$  is the solution

$$\bar{g}_{\mu\nu} = g_{\mu\nu} + 2\langle \chi_{\mu\nu} \rangle$$

Example :  $\mathcal{L}_{\text{HD}} = \frac{m}{2}(\dot{x}^2 - \tau^2 \ddot{x}^2) + x F_{\text{ext}}(t)$

$$m \frac{d^2}{dt^2} \left( 1 + \tau^2 \frac{d^2}{dt^2} \right) x = F_{\text{ext}}$$

invert with  $\mathcal{P} \frac{1}{1 + \tau^2 \frac{d^2}{dt^2}}$

The projected equation is

$$m \ddot{x} = \int_{-\infty}^{\infty} du \frac{\sin(|u|/\tau)}{2\tau} F_{\text{ext}}(t - u)$$

$$\tau \sim \frac{1}{m_x}$$

→ violation of microcausality

~~$$\vec{F} = m \vec{a}$$~~

$$\langle F \rangle = m a \quad !!$$

$$|u| \sim \tau$$



# The FLRW metric

$$ds^2 = g_{\mu\nu} dx^\mu dx^\nu = dt^2 - a^2(t) d\sigma^2$$

$$g_{\mu\nu}, \phi, \cancel{\chi_{\mu\nu}}$$

$$d\sigma^2 = \frac{dr^2}{1 - kr^2} + r^2 d\theta^2 + r^2 \sin^2 \theta d\phi^2$$

Unprojected equations  $\left( \frac{\mathcal{L}}{\sqrt{-g}} \sim R + R^2 \right)$

$$\Sigma \left( \frac{\ddot{a}}{a} + \frac{\dot{a}^2}{a^2} + \frac{k}{a^2} \right) = \frac{4\pi G}{3} (\rho - 3p), \quad \Upsilon \left( \frac{\ddot{a}}{a} - \frac{\dot{a}^2}{a^2} - \frac{k}{a^2} \right) = -4\pi G (\rho + p),$$

where

$$\Sigma = 1 + \frac{1}{m_\phi^2} \left( 3 \frac{\dot{a}}{a} + \frac{d}{dt} \right) \frac{d}{dt}, \quad \Upsilon = \Sigma + \frac{2}{m_\phi^2} \left[ \frac{k}{a^2} + 3 \frac{d}{dt} \left( \frac{\dot{a}}{a} \right) \right].$$

$$\square_{\text{cov}} - m_\phi^2$$

Projection. Define

$$\langle A \rangle_X \equiv \frac{1}{2} \left[ \frac{1}{X} \Big|_{\text{rit}} + \frac{1}{X} \Big|_{\text{adv}} \right] A$$

and use it to define  $\frac{1}{\Sigma}$  and  $\frac{1}{\Upsilon}$

(Partially) projected equations :



$$\frac{\ddot{a}}{a} + \frac{\dot{a}^2}{a^2} + \frac{k}{a^2} = \frac{4\pi G}{3} \langle \rho - 3p \rangle_{\Sigma}$$

$$\frac{\ddot{a}}{a} - \frac{\dot{a}^2}{a^2} - \frac{k}{a^2} = -4\pi G \langle \rho + p \rangle_{\Upsilon}$$

(it is NOT  
over yet  
.....!!!)

OR:

$$\frac{\dot{a}^2}{a^2} + \frac{k}{a^2} = \frac{8\pi G}{3} \tilde{\rho},$$
$$2\frac{\ddot{a}}{a} + \frac{\dot{a}^2}{a^2} + \frac{k}{a^2} = -8\pi G \tilde{p}.$$

where

$$\tilde{\rho} = \frac{1}{4} \langle \rho - 3p \rangle_{\Sigma} + \frac{3}{4} \langle \rho + p \rangle_{\Upsilon}$$
$$\tilde{p} = \frac{1}{4} \langle \rho + p \rangle_{\Upsilon} - \frac{1}{4} \langle \rho - 3p \rangle_{\Sigma}$$

The projection can be handled exactly for radiation combined with the vacuum energy:

$$p = \frac{\rho}{3} + p_0 \quad p_0 = \text{constant}$$

Exact solution:  $\rho_0 = 3\sigma^2/(8\pi G) \quad \tilde{p} = (\tilde{\rho} - 4\rho_0)/3$

$$\sigma, \sigma' = \text{constants}$$

$$\rho(t) = \frac{3}{8\pi G} \left( \sigma^2 + \frac{\sigma'^2}{4a^4} \right), \quad \sigma'^2 = \sigma'^2 \left( 1 + \frac{4\sigma^2}{m_\phi^2} \right) \quad \tilde{\rho}(t) = \frac{3}{8\pi G} \left( \sigma^2 + \frac{\sigma'^2}{4a^4} \right)$$

$$a(t) = \sqrt{\frac{\sinh(\sigma t)}{\sigma} \left( \sigma' \cosh(\sigma t) - \frac{k}{\sigma} \sinh(\sigma t) \right)}$$

But in general the projection is defined perturbatively  
(since it comes from quantum gravity, which is defined perturbatively)

→ The classical equations are defined perturbatively : one may have to face asymptotic series and nonperturbative effects  
(just to write the equations)

Example: cosmic dust ( $p = 0$ ) or  $p = w\rho$   
 $w \neq \frac{1}{3}, -1$

Example:

$$\mathcal{L}_{\text{HD}} = \frac{m}{2}(\dot{x}^2 - \tau^2 \ddot{x}^2) - V \quad V = \frac{m}{2}\omega^2 x^2 + \frac{\lambda}{4!}x^4$$

Unprojected equations of motion:

$$m\tilde{K} \left( \frac{d^2}{dt^2} + \Omega^2 \right) x = -\frac{\lambda x^3}{3!}$$

where

$$\Omega = \frac{1}{\tau\sqrt{2}}\sqrt{1 - \sqrt{1 - 4\tau^2\omega^2}}, \quad \tilde{\Omega} = \frac{1}{\tau\sqrt{2}}\sqrt{1 + \sqrt{1 - 4\tau^2\omega^2}}, \quad \tilde{K} = \tau^2\tilde{\Omega}^2 + \tau^2\frac{d^2}{dt^2}.$$

Projected equations of motion:

$$m \left( \frac{d^2}{dt^2} + \Omega^2 \right) x = -\frac{\lambda}{3!} \langle x^3 \rangle_{\tilde{K}} \quad \langle A \rangle_X \equiv \frac{1}{2} \left[ \frac{1}{X} \Big|_{\text{rit}} + \frac{1}{X} \Big|_{\text{adv}} \right] A$$

By iterating the projection, we get

$$\omega=0 \quad \tilde{\lambda} \equiv \lambda/m$$

$$\ddot{x} = -\frac{\tilde{\lambda}x}{6} (x^2 - 6\tau^2\dot{x}^2) - \frac{\tilde{\lambda}^2\tau^2x}{12} (x^4 - 48\tau^2x^2\dot{x}^2 + 372\tau^4\dot{x}^4) \\ - \frac{\tilde{\lambda}^3\tau^4x}{6} (x^6 - 156\tau^2x^4\dot{x}^2 + 4572\tau^4x^2\dot{x}^4 - 31152\tau^6\dot{x}^6) + \mathcal{O}(\tilde{\lambda}^4)$$

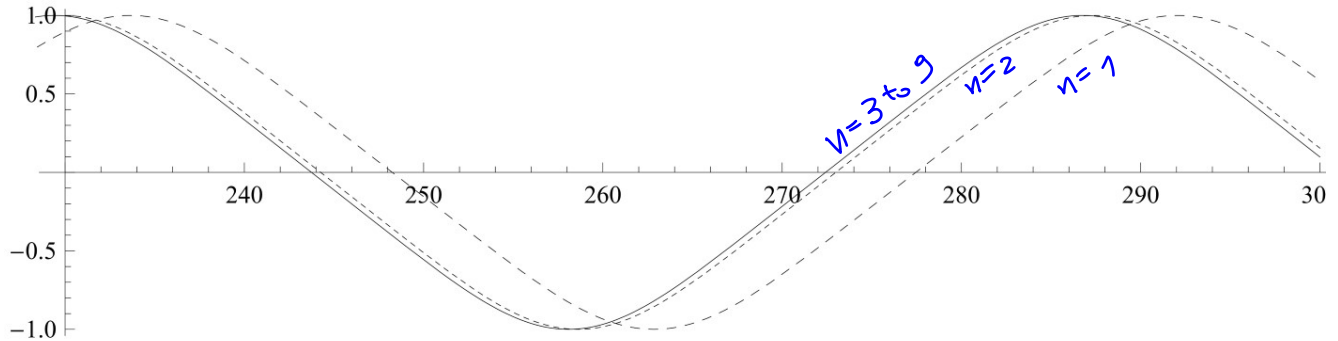
$$\frac{\mathcal{L}}{m} = \frac{\dot{x}^2}{2} - \frac{\tilde{\lambda}x^2}{4!} (x^2 + 12\tau^2\dot{x}^2) + \frac{\tau^2\tilde{\lambda}^2x^2}{72} (x^4 - 54\tau^2x^2\dot{x}^2 + 372\tau^4\dot{x}^4) + \mathcal{O}(\tilde{\lambda}^3)$$

Growth of  
the coefficients :

$n$	5	10	15	20	25
$c_{n,0}$	$10^0$	$10^6$	$10^{13}$	$10^{22}$	$10^{32}$
$c_{n,n}$	$10^9$	$10^{28}$	$10^{52}$	$10^{78}$	$10^{107}$

!!

Solution with  $x(0) = 1$ ,  $\dot{x}(0) = 0$ ,  $m = \tau = 1$ ,  $\lambda = \frac{1}{10}$



$n=1$  : fairly good

$n=2$  : good

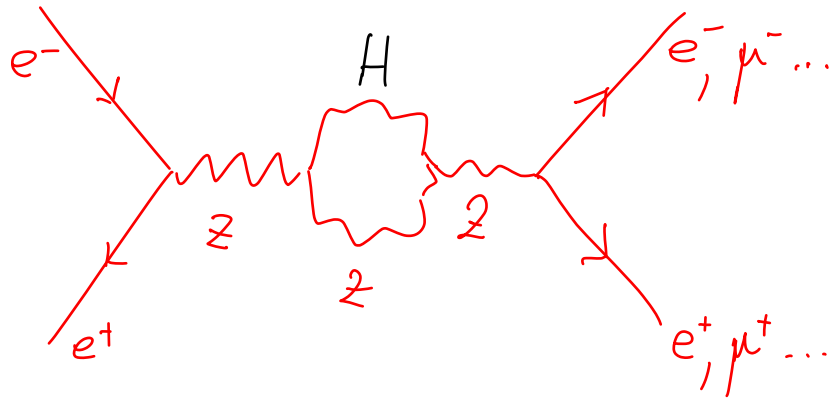
$n=3$  to  $n=9$  : excellent

$n > 9$  : meaningless



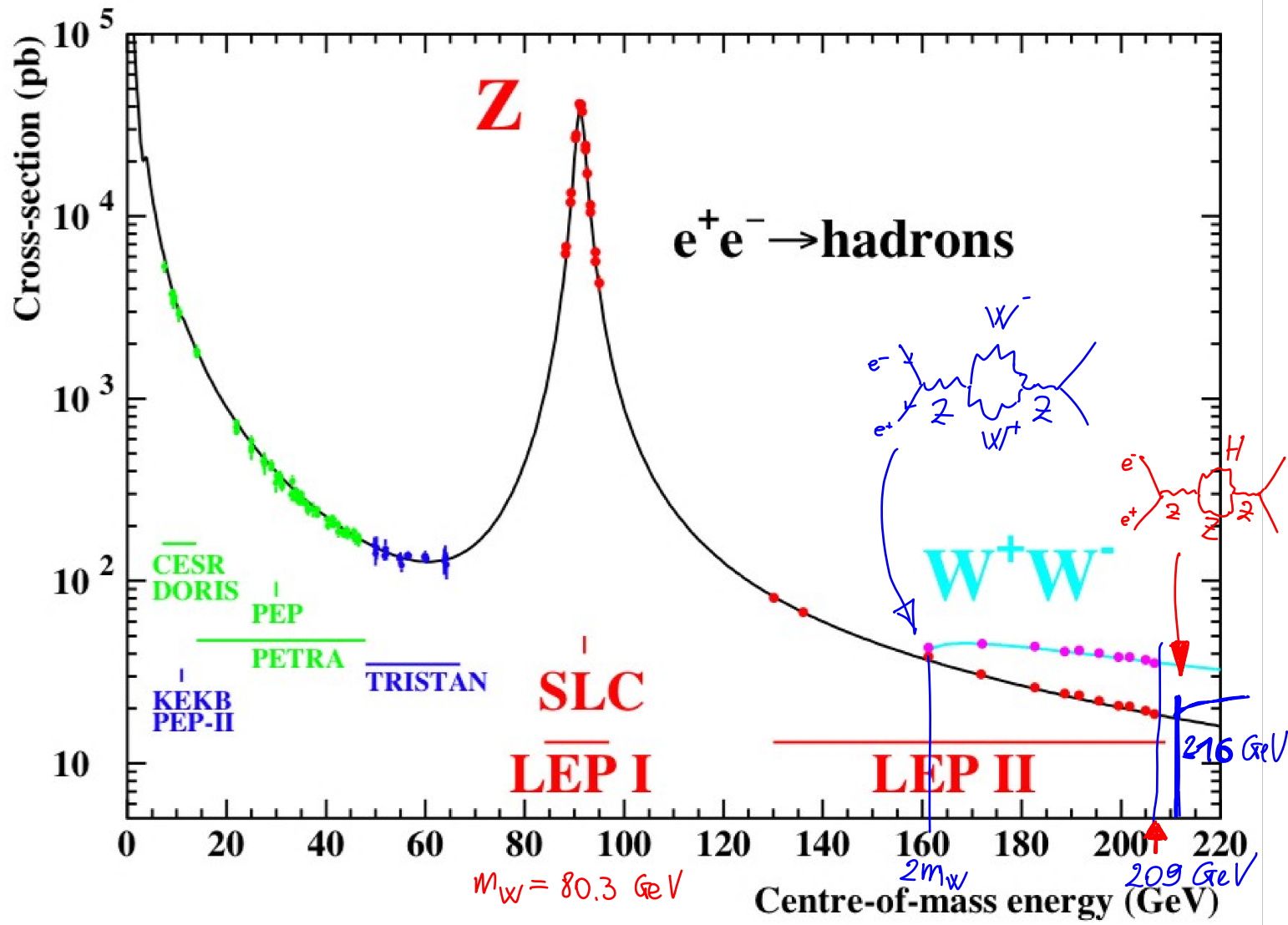
The fakeon prescription can be applied universally  
We should talk about "quantum field theory of particles and fakeons"

Is H a fakeon? Maybe...



$$m_H + m_Z = 216 \text{ GeV}$$

D. A., On the nature of the Higgs boson, MPLA 33 (2019) 1950123  
arXiv: 1811.02600 [hep-ph]



# Hoft - Veltman, Diagrammar, CERN 73-09, § 6.1

Every diagram, when multiplied by the appropriate source functions and integrated over all  $x$  contributes to the S-matrix. The contribution to the T-matrix, defined by

$$S = 1 + iT \quad (6.7)$$

is obtained by multiplying by a factor  $-i$ . Unitarity of the S-matrix implies an equation for the imaginary part of the so defined T matrix

$$T - T^\dagger = iT^\dagger T. \quad (6.8)$$

The T-matrix, or rather the diagrams, are also constrained by the requirement of causality. As yet nobody has found a definition of causality that corresponds directly to the intuitive notions; instead formulations have been proposed involving the off-mass-shell Green's functions. We will employ the causality requirement in the form proposed by Bogoliubov that has at least some intuitive appeal and is most suitable in connection with a diagrammatic analysis. Roughly speaking Bogoliubov's condition can be put as follows: if a space-time point  $x_1$  is in the future with respect to some other space-time point  $x_2$ , then the diagrams involving  $x_1$  and  $x_2$  can be rewritten in terms of functions that involve positive energy flow from  $x_2$  to  $x_1$  only.

The trouble with this definition is that space-time points cannot be accurately pinpointed with relativistic wave packets corresponding to particles on mass-shell. Therefore this definition cannot be formulated as an S-matrix constraint. It can only be used for the Green's functions.

Other definitions refer to the properties of the fields. In particular there is the proposal of Lehmann, Symanzik and Zimmermann that the fields commute outside the light cone. Defining fields in terms of diagrams, this definition can be shown to reduce to Bogoliubov's definition. The formulation of Bogoliubov causality in terms of cutting rules for diagrams will be given in Section 6.4.

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## Comments on alternative approaches to the problem of quantum gravity

--- **string theory** is criticized for being nonpredictive. Moreover, its calculations often require mathematics that is not completely understood

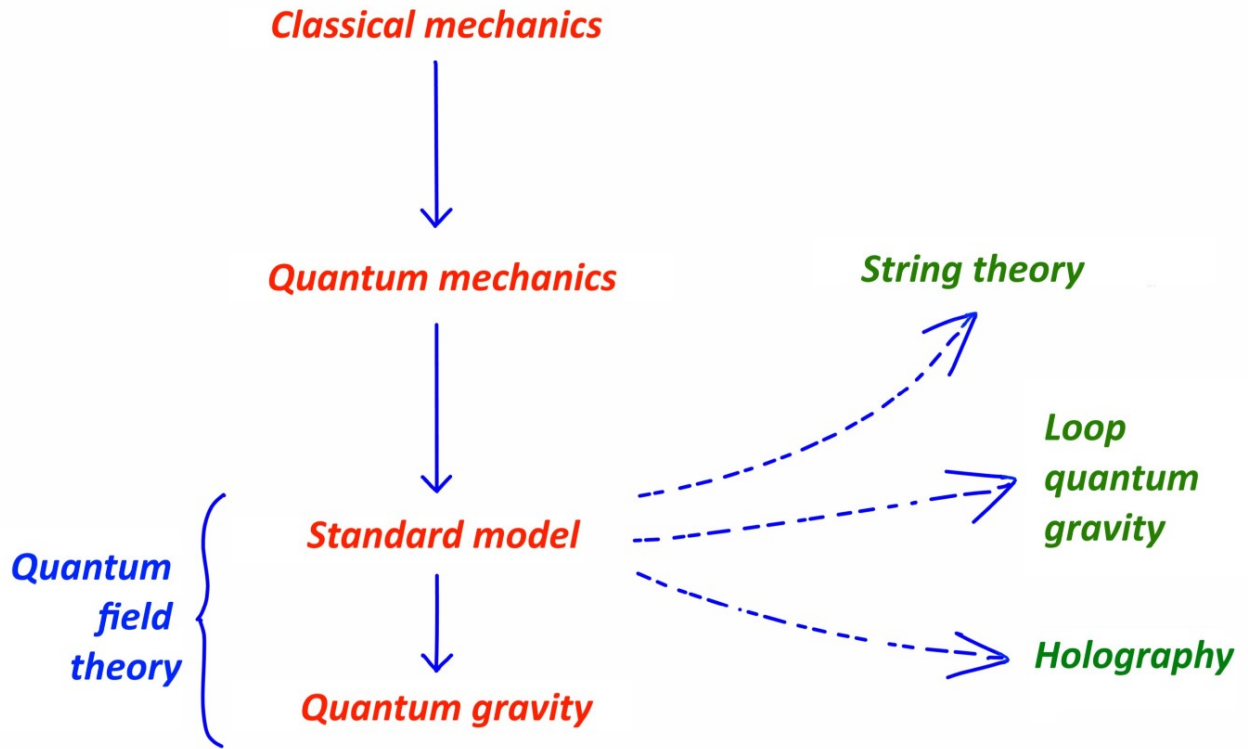
--- **loop quantum gravity** is even more challenging, because it is at an earlier stage of development

--- **holography** (AdS/CFT correspondence) do not admit a weakly coupled expansion

--- **asymptotic safety** in nonperturbative as well.

**None is as close to the standard model as the solution based on the fakeon idea, which is a quantum field theory, admits a perturbative expansion in terms of Feynman diagrams and allows us to make calculations with a comparable effort. It can be coupled to the standard model straightforwardly.**

**Our solution bests its competitors in calculability, predictivity and falsifiability. It is also rather rigid, because it contains only two new parameters. It could turn out to be the most predictive theory ever.**



QG is the "last mile" of the path to the infinitesimally small, right after the SM